

RABIN – KARP ALGORITHM

text: aaaaaaaaaaaaaaaaaaaaaaaaaabbb

pattern: aaaaab

text: aaaaaaaaaaaaaaaaaaaaaaaaaaabbb

pattern: aaaaab

✓✓✓✓✓X

text: aaaaaaaaaaaaaaaaaaaaaaaaaaaaaabbb

pattern: aaaaab



text: aaaaaaaaaaaaaaaaaaaaaaaaabbb

pattern: aaaaab

$$h(\text{aaaaaa}) = h_t$$

$$h(\text{aaaaab}) = h_p$$

text: aaaaaaaaaaaaaaaaaaaaaaa aaaaabbbb



pattern: aaaaab

$$h(\text{aaaaab}) = h_t$$

$$h(\text{aaaaab}) = h_p$$

Lay man approach to generate hash function.....

text: abcdefghijk

pattern: cdef

$$h(cdef) = h(3, 4, 5, 6) = 18 \checkmark$$

$$h(abcd) = h(1, 2, 3, 4) = 10$$

$$h(bcde) = h(abcd) - 1 + 5 = 10 - 1 + 5 = 14$$

$$h(cdef) = h(bcde) - 2 + 6 = 14 - 2 + 6 = 18 \checkmark$$

a	1
b	2
c	3
d	4
e	5
f	6
g	7
h	8
i	9
j	10
k	11

Demerits : same value can be generated for different values/permutations.

text: abcdefghijk

multiplier: 10^{n-1} where n is the character position from the right

$$\begin{aligned}h(\text{abcd}) &= h(1, 2, 3, 4) \\ &= 1 \cdot 10^3 + 2 \cdot 10^2 + 3 \cdot 10^1 + 4 \cdot 10^0 \\ &= 1000 + 200 + 30 + 4 = 1234\end{aligned}$$

a	1
b	2
c	3
d	4
e	5
f	6
g	7
h	8
i	9
j	10
k	11
...	

text: abcdefghijk

multiplier: 10^{n-1} where n is the character position from the right

$$\begin{aligned}h(abcd) &= h(1, 2, 3, 4) \\ &= 1*10^3 + 2*10^2 + 3*10^1 + 4*10^0 \\ &= 1000 + 200 + 30 + 4 = 1234\end{aligned}$$

$$\begin{aligned}h(bcde) &= (h(abcd) - 1*10^3) * 10 + 5 \\ &= (1234 - 1000) * 10 + 5 = 2345\end{aligned}$$

$$\begin{aligned}h(cdef) &= (h(bcde) - 2*10^3) * 10 + 6 \\ &= (2345 - 2000) * 10 + 6 = 3456\end{aligned}$$

a	1
b	2
c	3
d	4
e	5
f	6
g	7
h	8
i	9
j	10
k	11
...	

text: abcdefghijk

$$\begin{aligned}h(\text{abcd}) &= (1 \cdot 10^3 + 2 \cdot 10^2 + 3 \cdot 10^1 + 4 \cdot 10^0) \bmod 113 \\ &= (1234) \bmod 113 = 104\end{aligned}$$

$$\begin{aligned}h(\text{bcde}) &= (((h(\text{abcd}) - 1 \cdot 10^3 \bmod 113) \cdot 10) \bmod 113 + 5) \bmod 113 \\ &= (((104 - 96) \cdot 10) \bmod 113 + 5) \bmod 113 \\ &= (80 \bmod 113 + 5) \bmod 113 = 85\end{aligned}$$

$$\text{Sanity check: } (2000 + 300 + 40 + 5) \bmod 113 = 85$$

Code attached in a file in cc website